

2011 UCAT SUMMER STUDENT PROGRAM (USSP 2011)

FRESHLY CONDENSED GRAINS IN THE DUSTY DISKS OF EVOLVED MAIN SEQUENCE BE STARS

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BE STAR COMPARISONS

Herbig Ae/Be stars vs. Classical Ae/Be stars

Herbig Ae/Be stars	classical Ae/Be stars
pre-main sequence stars	evolved main sequence stars
in star forming regions	not in star forming regions

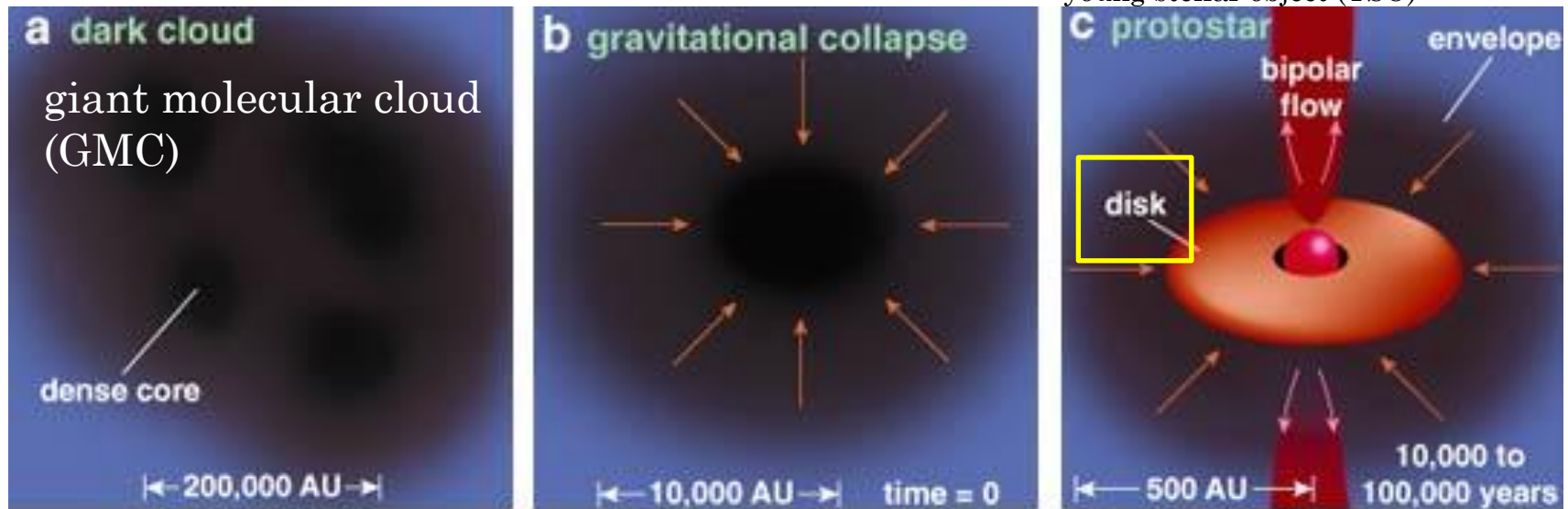


OUTLINE

- star formation
- pre-main sequence star comparisons
- Beckwith's model
- HD 259431 introduction
- estimation of disk mass – Beckwith
- estimation of disk mass – SED
- estimation of disk mass – T Tauri vs. Be stars
- discussion and conclusion



STAR FORMATION

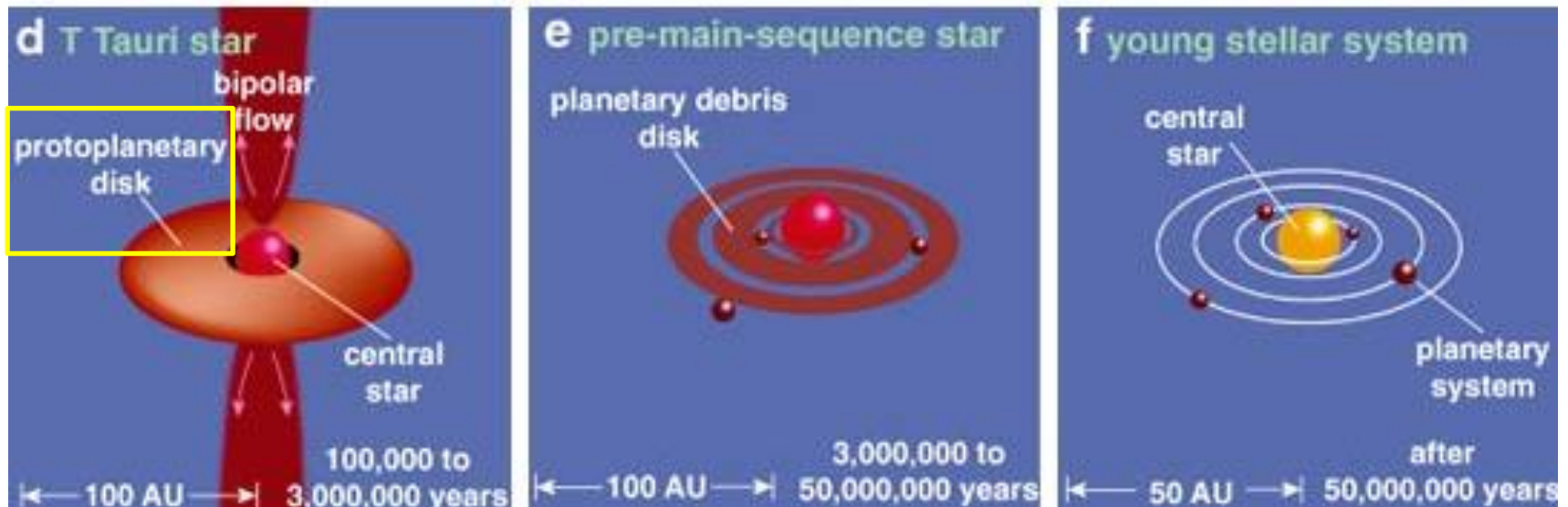


Greene, T., "Protostars", 2001, American Scientist, Vol.89, No.4

- Star formation begins inside dark interstellar clouds containing high-density regions that become gravitationally unstable and collapse under their own weight
- The collapsing core forms a protostar
- a phase of stellar evolution defined by the rapid accumulation of mass from a circumstellar disk and a surrounding envelope of gas and dust. As the dusty envelope dissipates, the object becomes visible at optical wavelengths for the first time as a T Tauri star

STAR FORMATION

young stellar object (YSO)



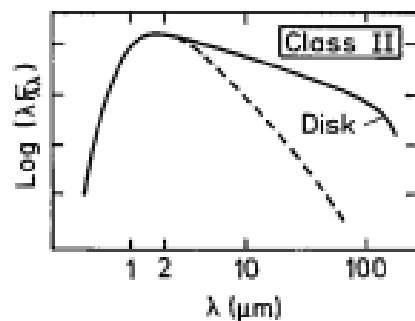
Greene, T., "Protostars", 2001, American Scientist, Vol.89, No.4

- d) These objects can often be recognized in telescopic images by the presence of a protoplanetary disk. After a few million years the dusty disk dissipates, leaving a bare pre-main-sequence star at its center
- e) In some instances, a debris disk with newly formed planets may continue to orbit the star. The star continues its gravitational collapse to the point where its core temperature becomes hot enough for nuclear fusion, and the object becomes a main-sequence star

PRE-MAIN SEQUENCE STAR COMPARISONS

T Tauri stars vs. Herbig Ae/Be stars

T Tauri stars	Herbig Ae/Be stars
pre-main sequence stars	
variable stars	
<2 Solar masses	2-8 Solar masses
F, G, K, M spectral type	spectral type earlier than F0



CLASS II:
Optically
thick
disk

Age $\sim 10^6$ yr
 $\langle M_{\text{disk}} \rangle \sim 0.01 M_\odot$

類日恆星誕生過程，《時空》第三十一期

BE STAR COMPARISONS

Herbig Ae/Be stars vs. Classical Ae/Be stars

Herbig Ae/Be stars	classical Ae/Be stars
pre-main sequence stars	evolved main sequence stars
infrared radiation excess due to circumstellar dust	infrared excess due to free-free emission
in star forming regions	not in star forming regions
	fast rotation
spectral type earlier than F0	
Balmer emission lines	



BECKWITH'S MODEL

Beckwith *et al.*, 1990

☉ spatially thin, axisymmetric disk

○ disk

$$T(r) = T_0 \left(\frac{r}{r_0}\right)^{-q}, \Sigma(r) = \Sigma_0 \left(\frac{r}{r_0}\right)^{-p}$$

$$L_\lambda = 4\pi\delta AB_\lambda(T)(1 - e^{-\tau_\lambda})$$

L_λ : luminosity density, F_λ : flux density

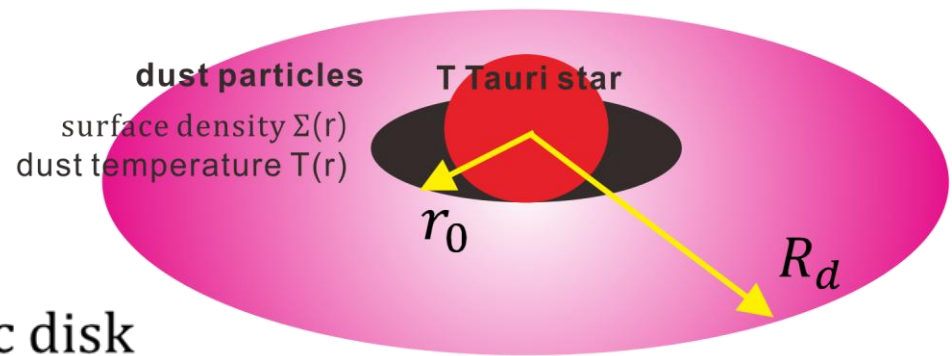
δA : projected area, $B_\lambda(T)$: Planck function

○ $L_\lambda \equiv 4\pi d^2 F_\lambda$, d : distance from the source

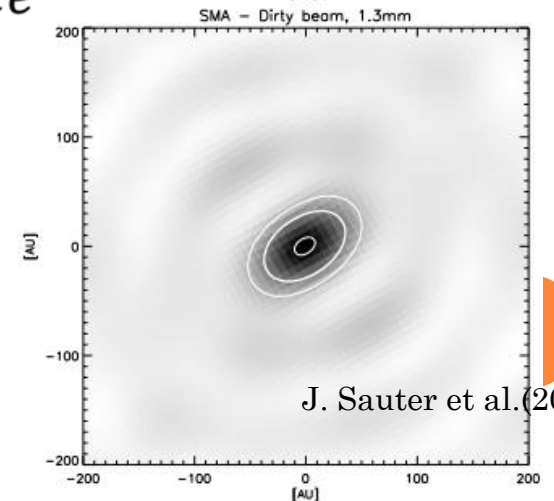
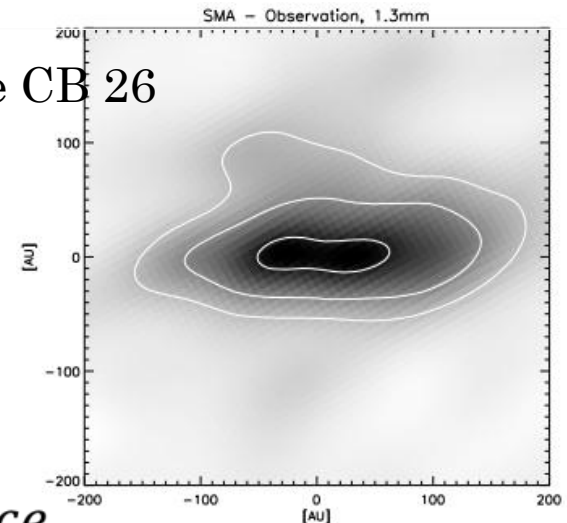
$$F_\lambda = \frac{\delta A}{4\pi d^2} \cdot 4\pi B_\lambda(T)\tau_\lambda$$

○ τ_λ : optical depth, $\tau_\lambda = \kappa_\lambda \Sigma \approx \kappa_\lambda \cdot \frac{M}{\delta A}$

$$M = \frac{F_\lambda d^2}{\kappa_\lambda B_\lambda(T)}, 1.3\text{mm}$$



Bok globule CB 26



J. Sauter et al. (2009)

INTRODUCE HD 259431

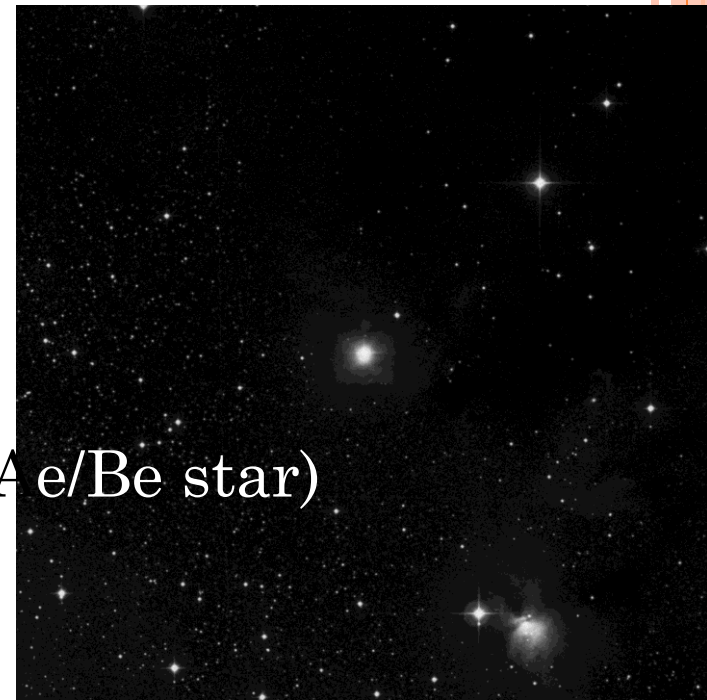
- HD 259431

variable star of Orion Type (Herbig Ae/Be star)

may be a classical Be star

spectral type: B3 (Swings & Struve, 1943)

distance: 800pc

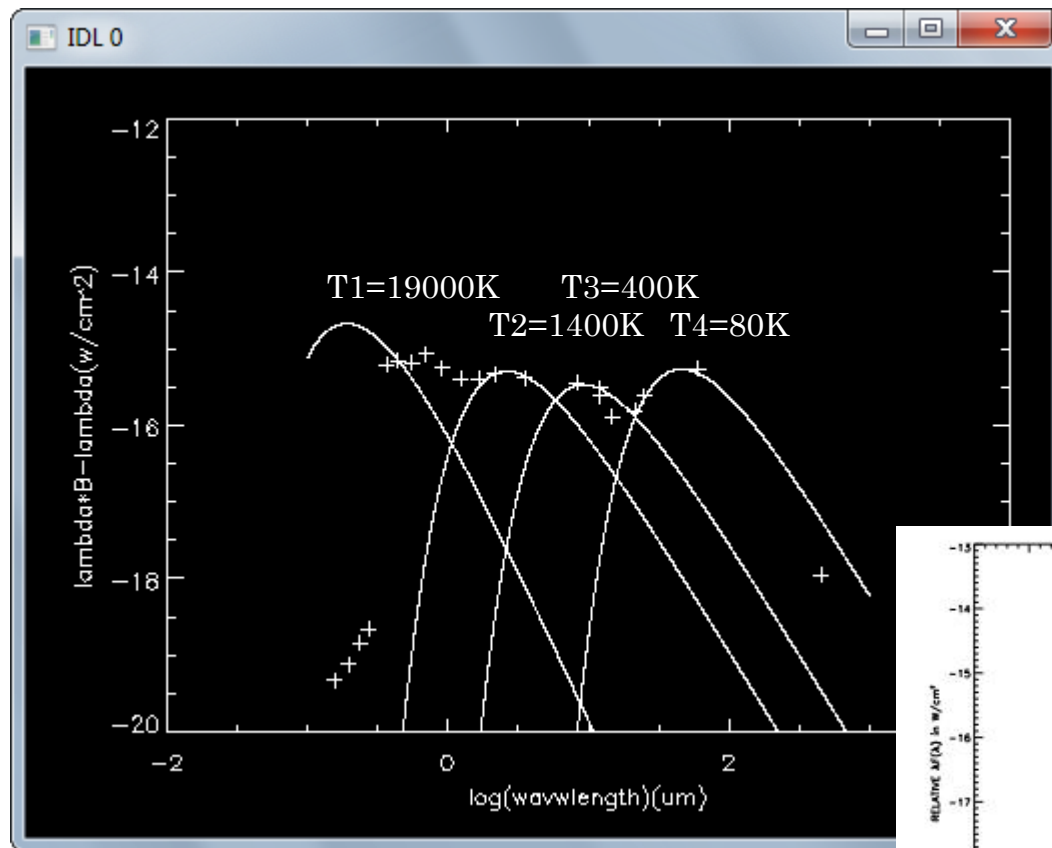


star	RA(2000)			Dec(2000)			SpT	V	J-H	H-K
	h	m	s	°	'	"		mag.	mag.	mag.
HD 259431	06	33	05.20	+10	19	19.9	B6	8.71	0.788	0.940

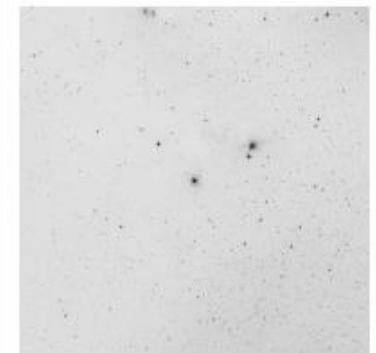
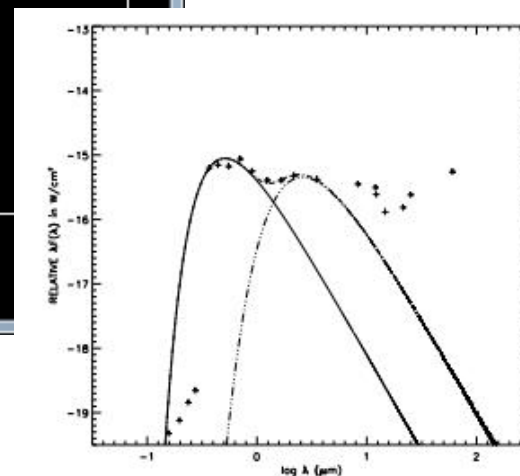
Near-Infrared Excess of Classical Be stars, 李建德(2009)



ESTIMATION OF DISK MASS



B3 star, $T_{\text{eff}}=19000K$
(Swings & Struve, 1943)



Near-Infrared Excess of Classical Be stars, 李建德(2009)

ESTIMATION OF DISK MASS – BECKWITH

- ③ flux density in 1.3mm(use blackbody, $T=80\text{K}$)

$$\text{when } \lambda = 1300\mu\text{m}, \lambda F_\lambda = 2.81 \times 10^{-19} \text{ W/cm}^2$$

$$F_\lambda = 2.16 \times 10^{-18} \text{ W/cm}^2$$

$$d = 800 \times 3.0857 \times 10^{16} \times 10^2 = 2.47 \times 10^{21} \text{ cm}$$

$$B_\lambda(80) = 2.16 \times 10^{-7} \text{ W/cm}^2$$

$$M_d = \frac{F_\lambda \times d^2}{\kappa_\lambda \times B_\lambda(T)} = 6.09 \times 10^{28} \times \kappa_\lambda^{-1}$$

- $\kappa_\lambda = \kappa_0 \left(\frac{\lambda_0}{\lambda}\right)^\beta$, while $\lambda_0 = 0.25\text{mm}$, $\kappa_0 = 0.1 \text{ cm}^2/\text{g}$
(Hildebrand, 1983)

- then get $\kappa_\lambda = 0.019 \text{ cm}^2/\text{g}$,

$$\text{and } M_d = 3.21 \times 10^{33} \text{ g} = 1.61 M_\odot$$



ESTIMATION OF DUST MASS – T TAURI VS. BE STARS

8 T Tau

distance: 140pc

flux density: 280mJy

$M_d: 0.016M_{\odot}$

○ HD 259431

distance: 800pc

flux density: $2.16 \times 10^{-18} \text{ W/cm}^3 = 1210 \text{ mJy}$

$M_d: 1.61M_{\odot}$

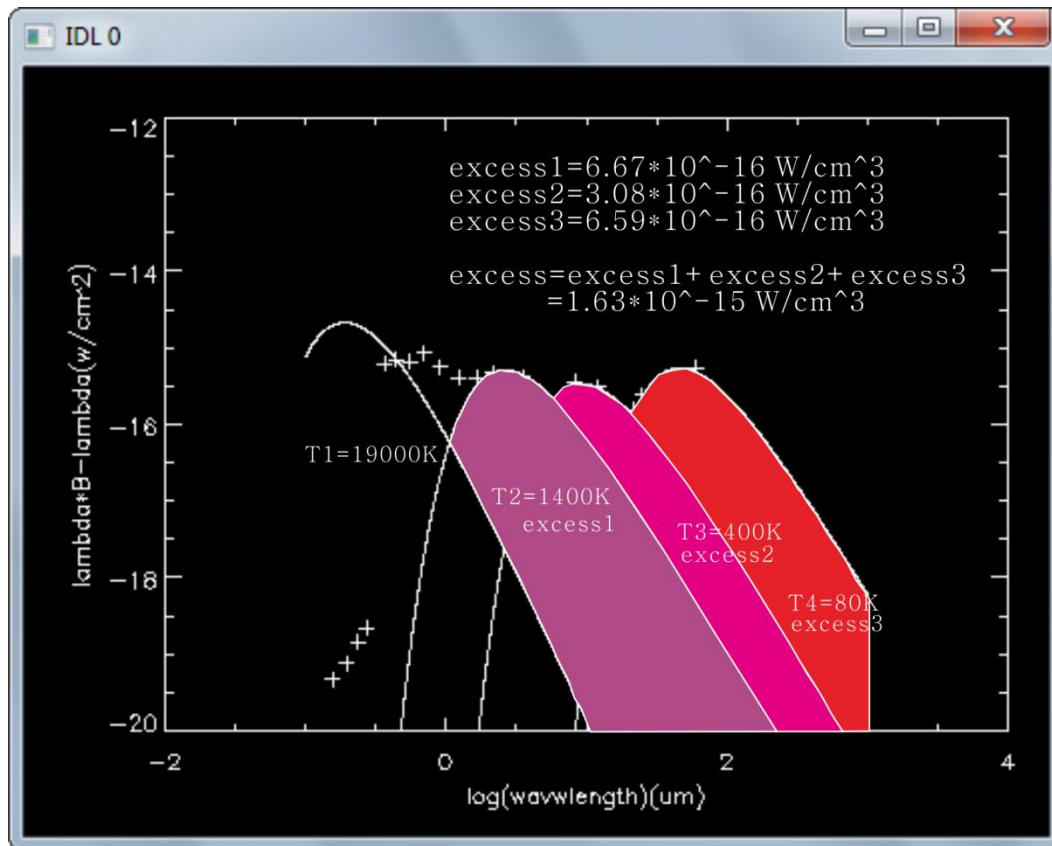
○ use $M = \frac{F_{\lambda} \times d^2}{\kappa_{\lambda} \times B_{\lambda}(T)}$

$$\text{left} = \frac{M_{d,HD\ 259431}}{M_{d,T\ Tau}} = 100.50$$

$$\text{right} = \frac{1210}{280} \times \left(\frac{800}{140}\right)^2 = 141.11$$



ESTIMATION OF DISK MASS – SED



```
主控台 X
% Compiled module: $MAIN$.
excess1= 6.6684123e-016
excess2= 3.0771061e-016
excess3= 6.5871561e-016
excess= 1.6332675e-015
```

T2=1400K	purple	1400K particles
T3=400K	pink	400K particles
T4=80K	red	80K particles



ESTIMATION OF DISK MASS – SED

- assume dust particles are silicate, a perfect sphere and an ideal black body
- radius: $r_s = 0.1\mu m$, volume: $V_s = 4.19 \times 10^{-21}(m^3)$
density: $d_s = 2\text{ }^g/cm^3(2000\text{ }^{kg}/m^3)$,
temperature: 80K(excess3), 400K(excess2), 1400K(excess1)
distance: $d=800pc=2.47 \times 10^{19}m$

Brian Donehew and Sean Brittain(2011)



ESTIMATION OF DISK MASS —

③ one particle:

$$L = 4\pi r_s^2 \sigma T_e^4, F_\lambda = \frac{L}{4\pi d^2}$$

$$80\text{K}, L = 2.92 \times 10^{-13} (W),$$

$$F_\lambda = 3.80 \times 10^{-53} (W/m^2) = 3.80 \times 10^{-57} (W/cm^2)$$

$$400\text{K}, L = 1.82 \times 10^{-10} (W),$$

$$F_\lambda = 2.37 \times 10^{-50} (W/m^2) = 2.37 \times 10^{-54} (W/cm^2)$$

$$1400\text{K}, L = 2.74 \times 10^{-8} (W),$$

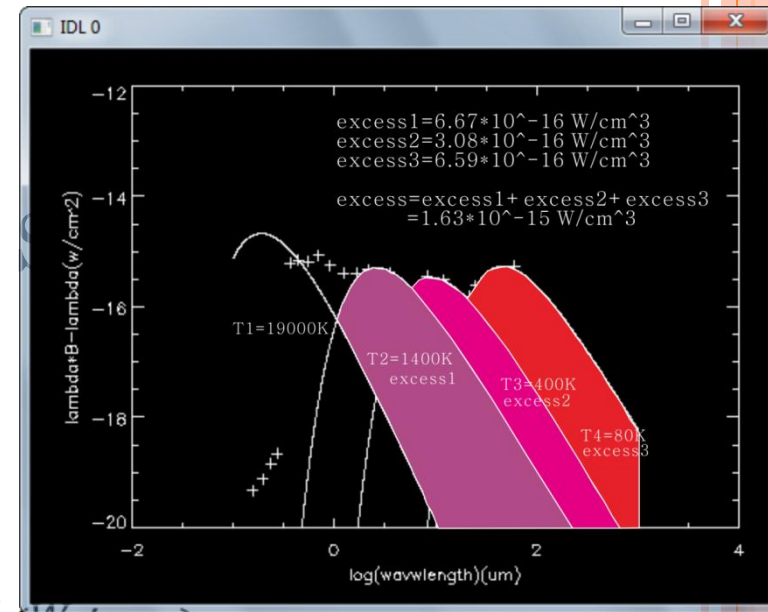
$$F_\lambda = 3.57 \times 10^{-48} (W/m^2) = 3.57 \times 10^{-52} (W/cm^2)$$

○ we have

$$\text{excess3}(80\text{K}) F_\lambda = 6.59 \times 10^{-16} (W/cm^2)$$

$$\text{excess2}(400\text{K}) F_\lambda = 3.08 \times 10^{-16} (W/cm^2)$$

$$\text{excess1}(1400\text{K}) F_\lambda = 6.67 \times 10^{-16} (W/cm^2)$$



- the particle number may be

$$N_3 = 1.73 \times 10^{41}$$

$$N_2 = 1.30 \times 10^{38}$$

$$N_1 = 1.87 \times 10^{36}$$

$$N_t = N_1 + N_2 + N_3 = 1.73 \times 10^{41}$$

- total mass of dust should be

$$M = N \times V_s \times d_s = 1.45 \times 10^{27} (g)$$

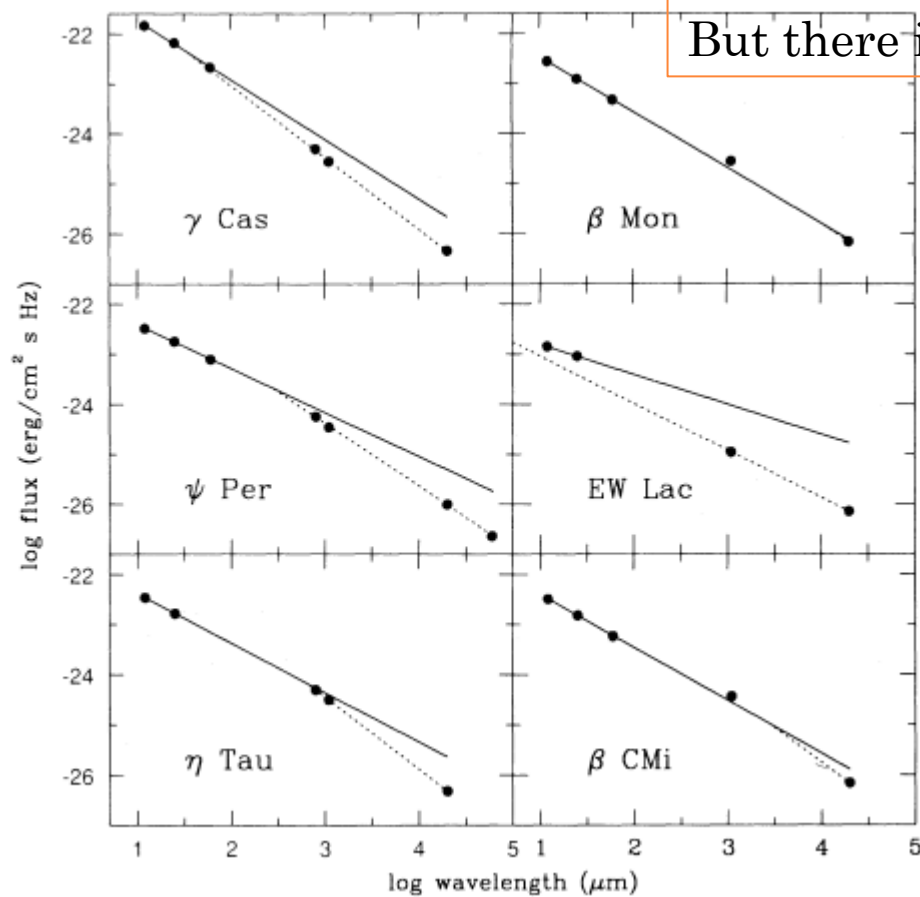
- typical ISM, gas to dust ratio is 100,

$$M_d = 1.45 \times 10^{29} (g) = 7.29 \times 10^{-5} M_{\odot}$$



DISCUSSION

○ Beckwith model vs. SED



But there is turn over must be considered...



DISCUSSION

- T Tau(T Tauri) $M_* = 1.91M_\odot$ $M_d = 0.016M_\odot$
HD 259431(Be star) $M_* = 6.4M_\odot$ $M_d = 7.29 \times 10^{-5} M_\odot$
- typical ISM: $M_{gas} \approx 100M_{dust}$

Be stars was thought to have lower mass of disk
because it is hotter



CONCLUSION

- opacity, κ_λ
- use a T Tauri star model
- use SED
- submillimeter and millimeter observation is a tool needed

ALMA!

Thanks for your listening!



⑧ κ_λ : opacity, $\kappa_\lambda = \kappa_0 \left(\frac{\lambda_0}{\lambda}\right)^\beta$

0.002 to 0.10 $\text{cm}^2 \text{g}^{-1}$ (Draine, 1989)

in $30\mu\text{m}$, can be determined, but in long wavelengths...
shape, fractal dimensions

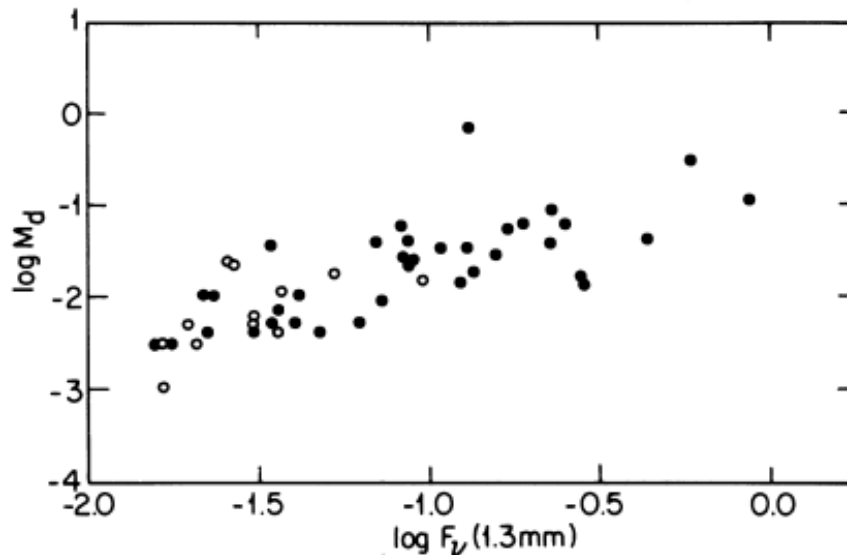


FIG. 5. Logarithm of derived disk mass M_d vs the 1.3 mm flux density F_ν shows the correlation of F_ν with total amount of emitting material; the scatter indicates variation in the disk temperatures that must be taken into account for an accurate derivation of M_d .

Beckwith *et al.*, 1990

ESTIMATION OF DISK MASS – SED

- 8 assume dust particles are silicate, a perfect sphere and an ideal black body

- radius: $r_s = 0.1\mu m$, volume: $V_s = 4.1888 \times 10^{-21}(m^3)$

density: $d_s = 2^g/cm^3(2000^{kg}/m^3)$,

temperature: 400K~1400K, 400K in average,

distance: $d=800pc$

Brian Donehew and Sean Brittain(2011)

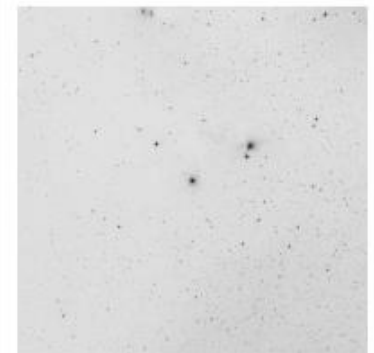
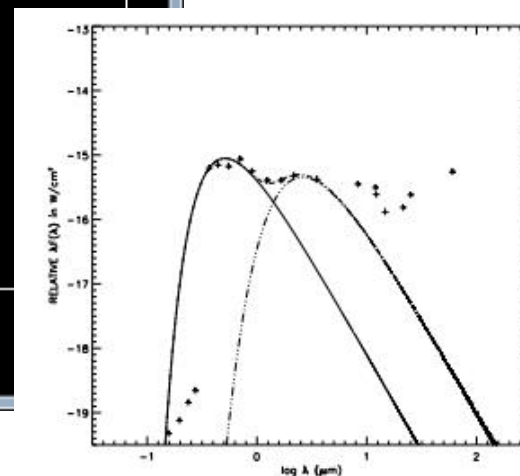
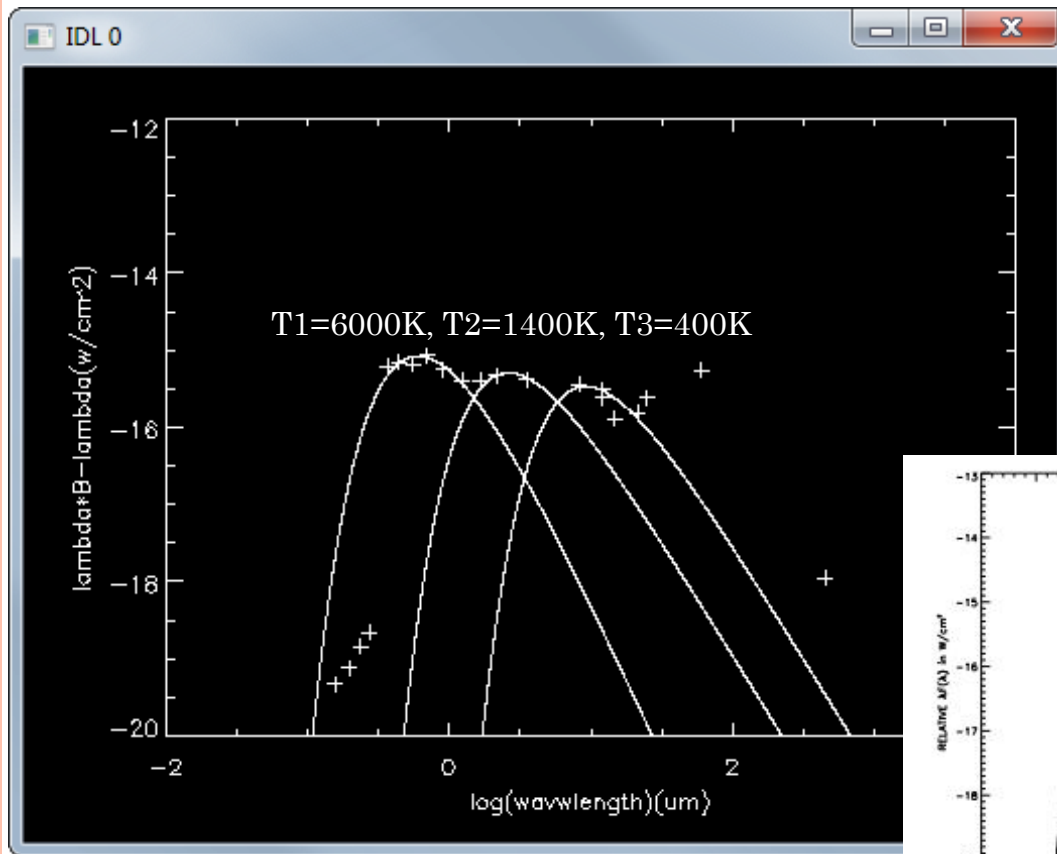
- one particle:

$$L=4\pi r_s^2 \sigma T_e^4 = 4.6751 \times 10^{-9}(W)$$

$$F_\lambda = \frac{L}{4\pi d^2} = 6.1052 \times 10^{-49}(W/m^2) = 6.1052 \times 10^{-53}(W/cm^2)$$

- we have total $F_\lambda = 8.5724 \times 10^{-16}(W/cm^2)$
- the particle number may be $N = 1.4041 \times 10^{37}$
- total mass of dust should be $M = N \times V_s \times d_s = 1.1763 \times 10^{23}(g)$
- typical ISM, gas to dust ratio is 100, $M_d = 1.1763 \times 10^{25}(g)$

ESTIMATION OF DISK MASS



Near-Infrared Excess of Classical Be stars, 李建德(2009)

ESTIMATION OF DISK MASS – BECKWITH

- ⑥ flux density in 1.3mm(use blackbody(T=400K))

$$\text{when } \lambda = 1300\mu m, \lambda F_{\lambda} = 4.0634 \times 10^{-23} W/cm^2$$

$$F_{\lambda} = 3.1257 \times 10^{-22} W/cm^3$$

$$d = 800 \times 3.0857 \times 10^{16} \times 10^2 = 2.4686 \times 10^{21} cm$$

$$B_{\lambda}(400) = 3.1260 \times 10^{-8} W/cm^3$$

$$M_d = \frac{F_{\lambda} \times d^2}{\kappa_{\lambda} \times B_{\lambda}(T)} = 6.0934 \times 10^{28} \times \kappa_{\lambda}^{-1}$$

- $\kappa_{\lambda} = \kappa_0 \left(\frac{\lambda_0}{\lambda}\right)^{\beta}$, while $\lambda_0 = 0.25mm$, $\kappa_0 = 0.1 cm^2/g$
(Hildebrand, 1983)

- then get $\kappa_{\lambda} = 0.019 cm^2/g$, and $M_d = 3.2071 \times 10^{30} g$



ESTIMATION OF DUST MASS — T TAURI VS. BE STARS

8 T Tau

distance: 140pc

flux density: 280mJy

M_d : $0.016M_{\odot}$

○ HD 259431

distance: 800pc

flux density: $3.1257 \times 10^{-22} \text{ W/cm}^3 = 0.17608 \text{ mJy}$

M_d : $0.0016M_{\odot}$

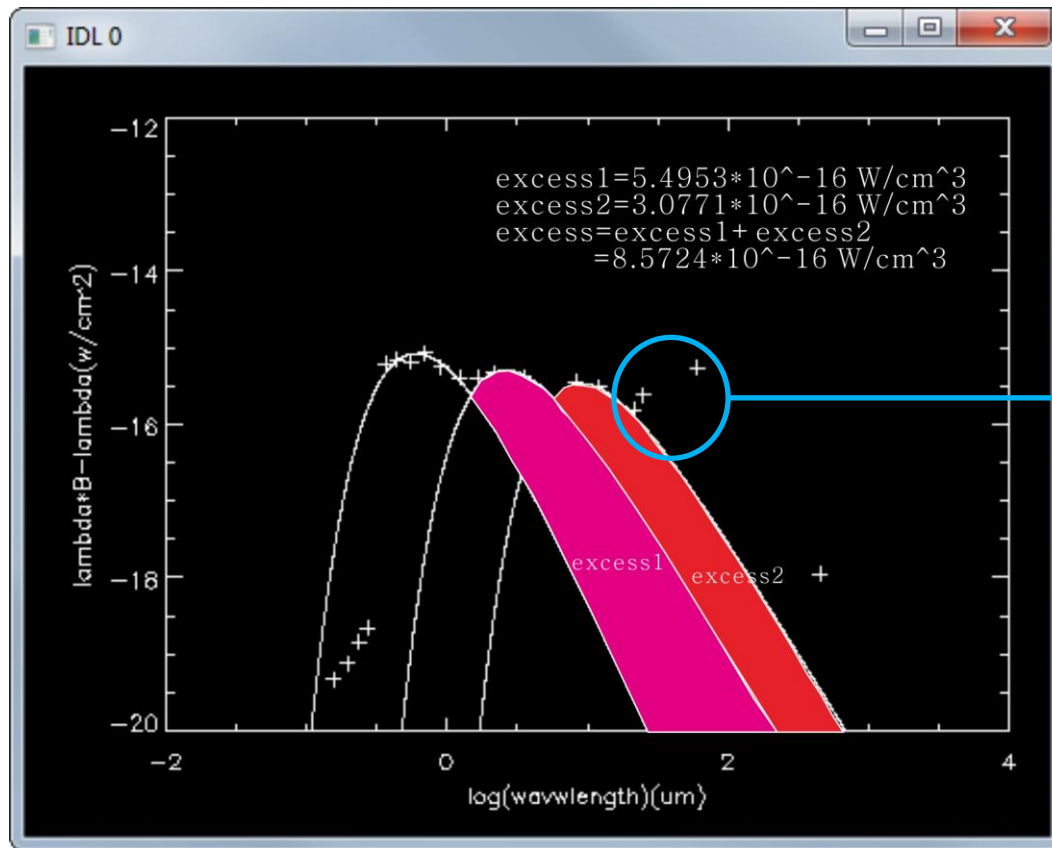
○ use $M = \frac{F_{\lambda} \times d^2}{\kappa_{\lambda} \times B_{\lambda}(T)}$

$$\text{left} = \frac{M_{d,HD\ 259431}}{M_{d,T\ Tau}} = 0.1$$

$$\text{right} = \frac{0.17608}{280} \times \left(\frac{800}{140}\right)^2 = 0.021$$



ESTIMATION OF DISK MASS – SED



```
主控台 X
% Compiled module: $MAIN$.
excess1=  5.4952784e-016
excess2=  3.0771061e-016
excess=  8.5723845e-016
```

There is not enough points to find another blackbody, indicating there is more IR excess. The disk mass estimated below is only the minimum



ESTIMATION OF DISK MASS – SED

- 8 assume dust particles are silicate, a perfect sphere and an ideal black body

- radius: $r_s = 0.1\mu m$, volume: $V_s = 4.1888 \times 10^{-21}(m^3)$

density: $d_s = 2\text{ }^g/cm^3(2000\text{ }^kg/m^3)$,

temperature: 400K~1400K, 900K in average,

distance: $d=800pc$

Brian Donehew and Sean Brittain(2011)

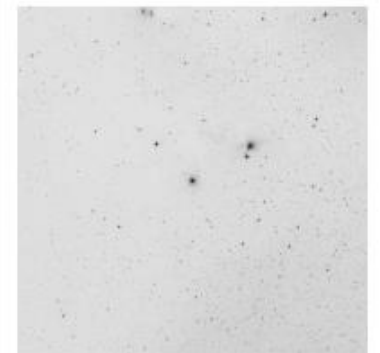
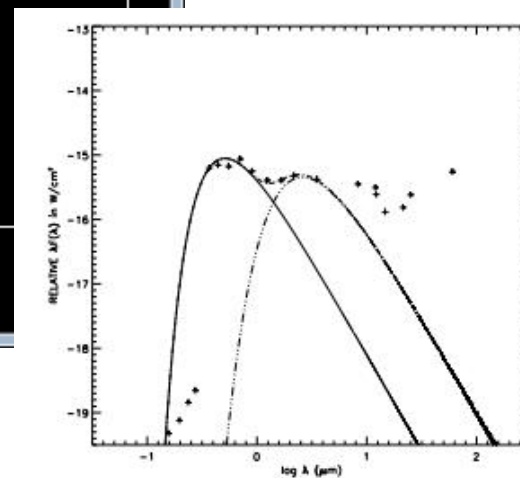
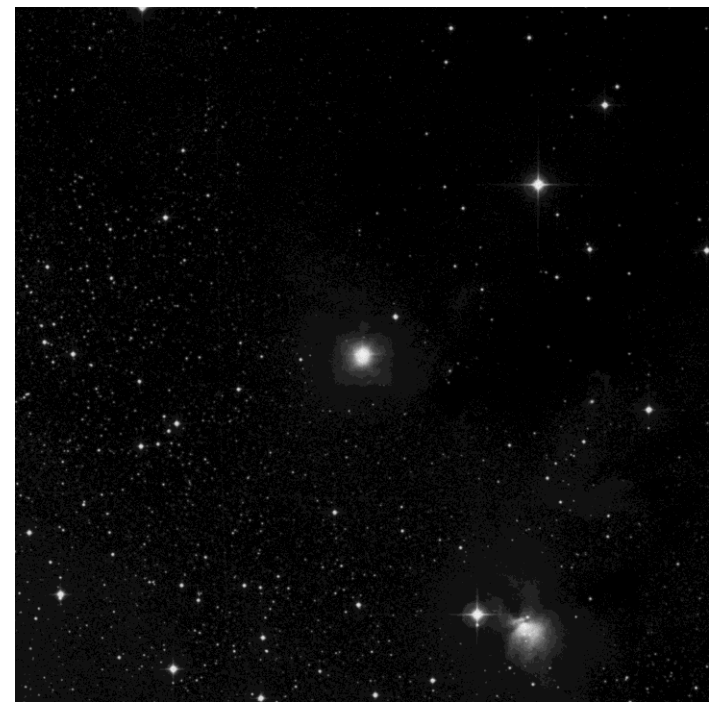
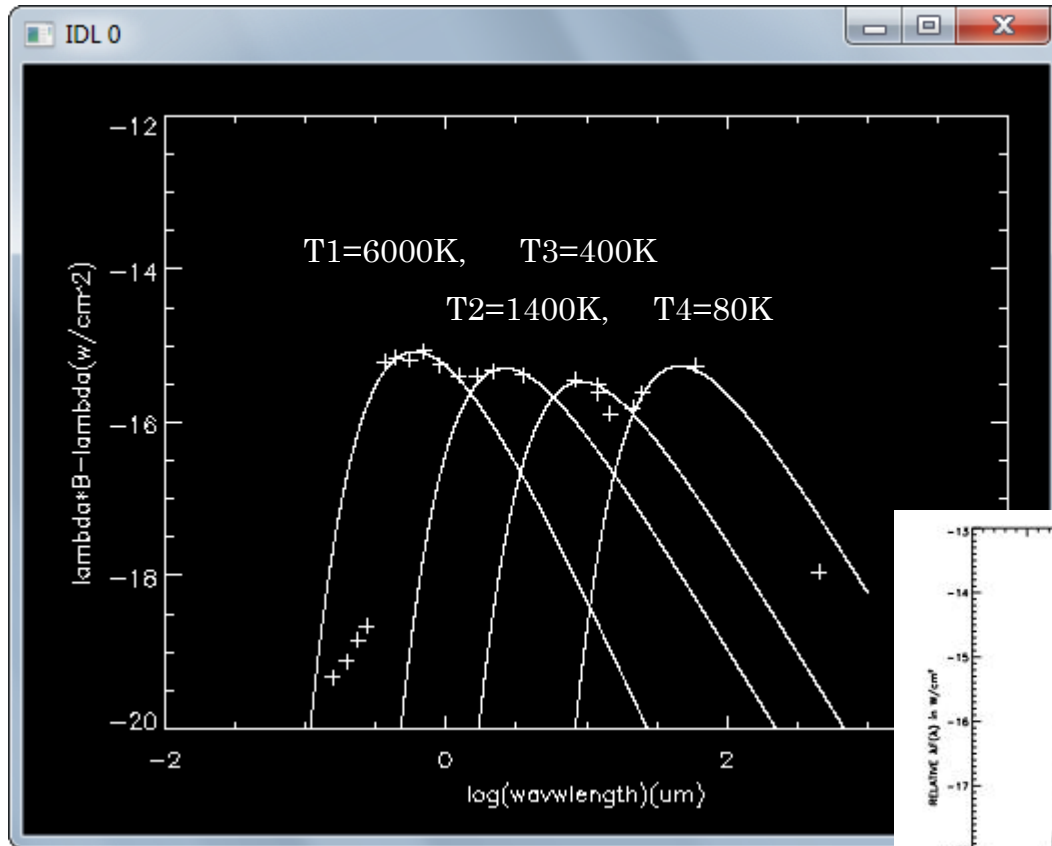
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- we have total $F_\lambda = 8.5724 \times 10^{-16}(W/cm^2)$
- the particle number may be $N = 1.4041 \times 10^{37}$
- total mass of dust should be $M = N \times V_s \times d_s = 1.1763 \times 10^{23}(g)$
- typical ISM, gas to dust ratio is 100, $M_d = 1.1763 \times 10^{25}(g)$

ESTIMATION OF DISK MASS



Near-Infrared Excess of Classical Be stars, 李建德(2009)

ESTIMATION OF DISK MASS – BECKWITH

- ⑥ flux density in 1.3mm(use blackbody($T=400K$))

$$\text{when } \lambda = 1300\mu m, \lambda F_{\lambda} = 2.8119 \times 10^{-19} W/cm^2$$

$$F_{\lambda} = 2.1632 \times 10^{-18} W/cm^3$$

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$$B_{\lambda}(80) = 2.1634 \times 10^{-7} W/cm^3$$

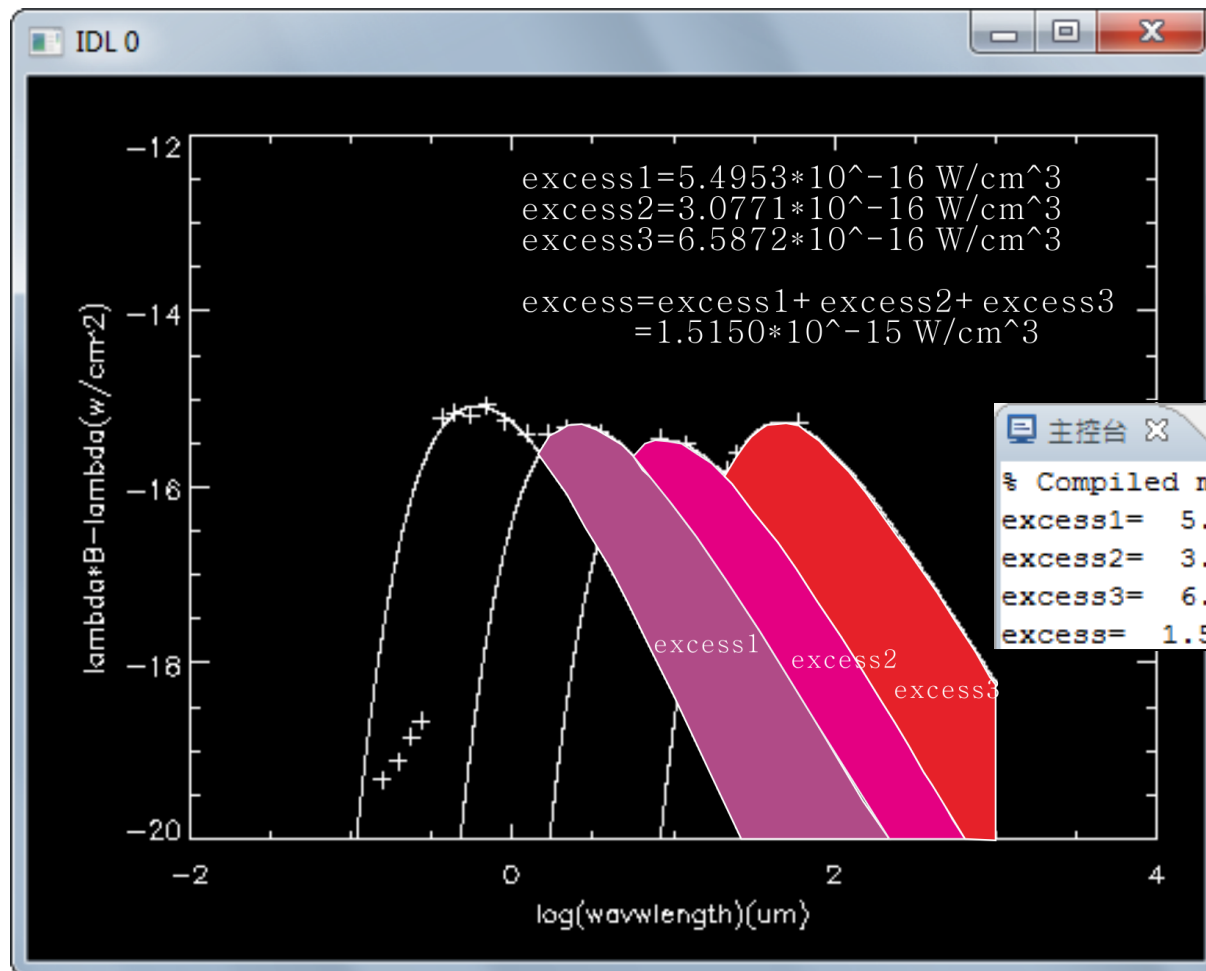
$$M_d = \frac{F_{\lambda} \times d^2}{\kappa_{\lambda} \times B_{\lambda}(T)} = 6.0934 \times 10^{28} \times \kappa_{\lambda}^{-1}$$

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(Hildebrand, 1983)

- then get $\kappa_{\lambda} = 0.019 cm^2/g$, and $M_d = 3.2071 \times 10^{33} g$



ESTIMATION OF DISK MASS – SED



主控台 X

```
% Compiled module: $MAIN$.  
excess1= 5.4952784e-016  
excess2= 3.0771061e-016  
excess3= 6.5871561e-016  
excess= 1.5159541e-015
```



ESTIMATION OF DISK MASS – SED

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density: $d_s = 2\text{ }^g/cm^3(2000\text{ }^{kg}/m^3)$,

temperature: 80K~1400K, 740K in average,

distance: $d=800pc$ Brian Donehew and Sean Brittain(2011)

- one particle:

$$L=4\pi r_s^2 \sigma T_e^4 = 2.1367 \times 10^{-9}(W)$$

$$F_\lambda = \frac{L}{4\pi d^2} = 2.7903 \times 10^{-49} (W/m^2) = 2.7903 \times 10^{-53} (W/cm^2)$$

- we have total $F_\lambda = 1.5160 \times 10^{-15} (W/cm^2)$
- the particle number may be $N = 5.4331 \times 10^{37}$
- total mass of dust should be $M = N \times V_s \times d_s = 4.5516 \times 10^{23}(g)$
- typical ISM, dust to gas ratio is 100, $M_d = 4.5516 \times 10^{25}(g)$